

pp. 106, Exercise Set 3.1

4. a. $Q(2)$: $2^2 \leq 30$ - true because $2^2 = 4$ and $4 \leq 30$,
 $Q(-2)$: $(-2)^2 \leq 30$ - true because $(-2)^2 = 4$ and $4 \leq 30$
 $Q(7)$: $7^2 \leq 30$ - false because $7^2 = 49$ and $49 \not\leq 30$,
 $Q(-7)$: $(-7)^2 \leq 30$ - false because $(-7)^2 = 49$ and $49 \not\leq 30$
c. truth set = $\{n \in \mathbf{Z}^+ \mid n^2 \leq 30\} = \{1, 2, 3, 4, 5\}$
10. Counterexample 1: Let $a = 1$, and note that $(a - 1)/a = (1 - 1)/1 = 0$ is an integer.
Counterexample 2: Let $a = -1$, and note that $(a - 1)/a = (-1 - 1)/(-1) = 2$ is an integer.
32. b. This statement translates as "For all real numbers x , if $x > 2$ then $x^2 > 4$," which is true.
d. This statement translates as "For all real numbers x , $x^2 > 4$ if, and only if, $|x| > 2$." This is true because $x^2 > 4$ if, and only if, $x > 2$ or $x < -2$, and $|x| > 2$ means that either $x > 2$ or $x < -2$.

pp. 116, Exercise Set 3.2

3. b. \exists a computer C such that C does not have a CPU.
d. \forall bands b , b has won fewer than 10 Grammy awards.
4. b. Some people are unhappy.
d. All estimates are inaccurate. *Or*: No estimates are accurate.
17. \exists an integer d such that $6/d$ is an integer and $d \neq 3$.
27. *Converse*: \forall integers d , if $d = 3$ then $6/d$ is an integer.
Inverse: \forall integers d , if $6/d$ is not an integer, then $d \neq 3$.
Contrapositive: \forall integers d , if $d \neq 3$ then $6/d$ is not an integer.
The converse and inverse of the statement are both true, but both the statement and its contrapositive are false. For example, when $d = 2$, then $d \neq 3$ but $6/d = 3$ is an integer.
42. If a person does not pass a comprehensive exam, then that person cannot obtain a master's degree. *Or*: If a person obtains a master's degree then that person passed a comprehensive exam.